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# Review of Underground Storage Tank Condition Monitoring Techniques

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**Abstract.** This article aims to provide a comprehensive review on the condition monitoring techniques of underground storage tanks (UST). Generally, the UST has long been a favourite toxic substance reservation apparatus, thanks to its large capacity and minimum floor space requirement. Recently, attention has been drawn to the safety risks of the complex cylindrical-shaped system and its surrounding environment due to contamination resulting from unwanted subsurface leakage. Studies on related countermeasures shows that numerous efforts have been focused on the damage remediation process and fault detection practice; however, it has also been observed that there are uncertainties in present technical complications involving the effectiveness of corrective actions and the robustness of condition monitoring techniques. As an alternative means to deliver spatial information on structural integrity, the feasibility of integrating non-destructive evaluation (NDE) techniques with machine learning algorithms, on observing the degradation process of UST, so as to enhance condition monitoring competency, is discussed.

#### 1 Introduction

Energy supply plays a crucial role by ensuring consumption sufficiency of a device over time to sustain an industry activity without disruption. Ranging from non-renewable coal, liquid fuel for transportation vehicles, to natural cooking gas, energy sources are categorized as hazardous substances, with flammability, corrosiveness, and chemical reactivity amongst the common traits. The mentioned toxic characteristics are also applied to industrial by-product such as radioactive waste and carbon dioxide  $(CO_2)$  [1]. Therefore, strict material-handling management and operation monitoring assessment are usually employed to prevent waste leakage, which would further evolve into undesirable intolerant faults, performance underachievement, environmental pollution and periods of downtime.

Underground storage tanks (UST) have been widely accepted for spacious energy supply reserves, refuelling and waste containments purposes. Typically found underneath petrol stations, laundry outlets and local households, the complex cylindrical-shaped containers are inevitably expose to contamination, corrosion and erosion during service periods [2-5]. Usually, the aforementioned deterioration signs focus on risk-bounded areas, including welding joints, tank bottoms, manholes, pumps and piping systems as displayed in Fig. 1 [6,7]; this deterioration arises due to harsh operating surroundings, metal and liquid reactions, specific material gravity difference of liquid and tank walls, fatigue, mismanagement and fault installation [8-10].

Additionally, the underground operating nature of UST is a double-edged sword: it offers low surface area requirements but consequently induces a certain degree of monitoring difficulty. An enormous amount of research has been carried out since the norm of inspection practice such as the cathodic protection method [11] are acknowledged to be costly, labourdemanding in long term, and inadequate in providing spatial information on the state of complex UST system as a whole [12]. The study area is comprised of remediation processes and fault detection monitoring techniques targeting hazardous contents multidisciplinary approach. Further elaboration presented in the section UST Condition Monitoring Techniques.

Nonetheless, several unpleasant incidents including the Gulf of Mexico oil spill [13,14] and Fukushima nuclear plant leakage [15,16] have recently caused legal disputes, incurring additional costs and unpredictable technical situations. Furthermore, the uncertainties in the present aging equipment risk assessment have publically raised skepticism on environment safety.

Adoption of an outdated or least rigorous condition monitoring technique at a hostile operating environment, together with heavy reliance on individual know-how and past experience amongst identified factors which contributes to undesirable events involving UST. Analysis of a total of 242 recorded UST damages lead to the conclusion that 30% of accident are preventable with quality maintenance and operations management [17]. It is believed there is rooms to improve existing

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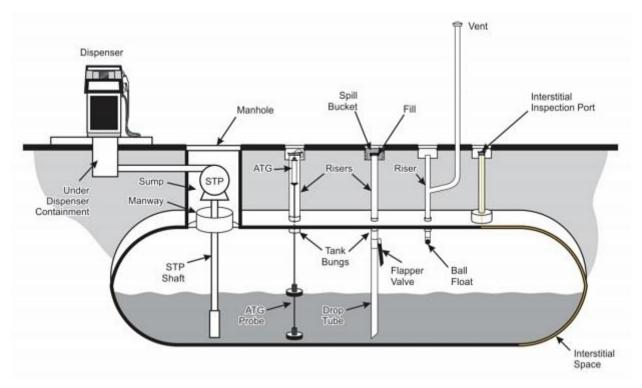


Fig. 1. General Petrol UST and Refueling Facility at Petrol Station

condition monitoring solutions for USTs after identifying the challenges and limitations. The viability of a product life cycle prediction and fault diagnosis model based on NDE techniques and machine learning algorithms will be tabulated in the Recommendations section.

### 2 UST Condition Monitoring Techniques

A variety of significant conventional monitoring techniques have been designed to cater for wide-range applications for different occasions. Notably, visual inspection performed by experienced personnel is suitable for preliminary analysis [18,19]. For ferrous and non-ferrous segments, oil and debris analysis is useful to detect any chips, leakage, or places where the coating may have detached [20-22]. By employing fundamental heat transfer theory, the thermography method screens structural temperature variation with respect to material properties and conductivity [23,24]. An on-line parameter tracking administration, namely Supervisory Control and Data Acquisition (SCADA) is specialized in wide coverage tribological monitoring [25,26]. Together with capacious data storage, SCADA's centralized control system is capable of providing an extensive review of multiple equipment or spacious facilities over time. Vibration-based analysis vet another distinctive option due to its well-established high-speed component fingerprint pattern recognition and diagnosis [27,28].

Despite proven success for the above methodologies, they are relatively inconvenient to apply to UST because of UST's restricted, difficult-to-reach underground environment characteristics. Also, due to the fact that an UST is a system influenced by multitudinal factors, straightforward conventional techniques would most

likely underestimate the black box model. In addition, the low correlation between time-varying factors and relatively time-consuming filling-discharge cycle periods add to the tedious computation and slow response. Taking into account the static nature of components together with the numerous dynamic attributes of product such as the liquid volumetric flow rate, USTs are rather insensitive to motion-type monitoring. For these collective investigation into condition reasons, monitoring techniques has been performed accommodate environmental hostility and decode the scarce available signals, both factors happening as a result of unresponsiveness from subsurface structures. milestones and findings available multidisciplinary studies will be described in a chronological order as below.

# 2.1 UST Condition Monitoring Research Development

Since last century, UST related condition monitoring research effort has been concentrates in several dimensions. For example, estimation of a risk-based parameter of a leaking tank was conducted by employing clean-up level approximation [29]. The transient behaviour of concentration output as described in an arbitrary-defined risk as time function is considered to be strongly subjective. A Fourier Transform infrared photacoustic spectroscopy analysis was introduced to probe UST nuclear waste [30]. In this case study, a convenient resolution on reactive waste detection with minimal hazardous pollutant handling was determined. The feasibility of utilizing commercial computational modelling methods in  $CO_2$  injection and containing process was compared under a test situation [31]. The

capability of a list of software was discussed and improvement proposed. The Electrical Resistance Tomography (ERT) technique was deployed to conduct a UST leakage detection test [32]. To assist leakage examination, a set of evenly-distributed electrode sensor arrays generated visualization via periodic sampling of tank waste amounts.

An interdependence of temperature changes between a tank wall, its surrounding, and the liquid inside was observed during an UST temperature-control simulation using Complex Finite Fourier Transform (CFFT) [33]. The UST thermal energy regulating model also implies system response is influenced by operating conditions. An online soil-venting system was studied to remedy petrol leakage [34]. Thorough information on leakage occurrence was recorded, particularly during refuelling activity; and the cost-effectiveness of moving towards zero-emission soil is reviewed. A reusable compound, HDTMA (hexadecyl-trimethylammonium)kaolin was introduced as an isolation material in case of contamination [35]. The hydraulic connectivity and ability to absorb petroleum chemical possessed by HDTMA-kaolin compound is comparable with a standard bentonite mixture.

An event of UST floating roof damage was simulated by incurring liquid sloshing as a result of lengthy high seismic amplitude effects [36]. Aiming to resemble the aftermath of an earthquake, the damage prediction is enhanced by taking into account neighbouring sediments, deep basin structure and source distance of ground motion. An optic fibre mid-infrared filtering technique was applied to examine CO<sub>2</sub> underground displacement and leakage monitoring Investigations has proven that it is practical to inspect gas admission and emission by referring to appropriate infrared characteristics: the wavelength range threshold, optical path compatibility, and optical fibre types.

An UST design review based on extreme stress analysis was carried out in the wake of a collapsed roof incident [38]. A strain gauge experimental dataset was collected under various stress tabulation settings to numerically assess the impact of structure geometry and corrosion distribution. A similar tank stress experiment has recommended weld toe geometry reinforcement in order to reduce local stresses [39]. Meanwhile, it has been observed that non-destructive Acoustic Emission (AE) signal analysis is engaged with a vertical UST floor plate scanning application [40]. The online monitoring of defects, for instance corrosion and leakage has been well-received since inactive time is no longer required.

In France, technology transfer from mining field to underground toxic gas constrained monitoring was implemented [41]. The following have proven to be efficient  $CO_2$  tracking options: a dynamic accumulation chamber located between soil and ambience for influx gas measurement; and an integrated gas sensor system gauging  $CO_2$  concentration at pit subsurface. The author emphasised that several gas parameters such as isotopic and composition influence the identification process. A type of optic fibre sensory array, namely Fibre Bragg Grating (FBG), was adopted in UST finite element

model online condition monitoring [42]. The proportional relationship between strain and FBG's wavelength variation reflects tank-bottom thickness loss caused by corrosion and wall vibration response.

The Environmental Results Program (ERP) assistant tools have been proposed with the aim to reduce frequency of UST structural inspection [43]. While the plan concentrates on addressing the risk of water supply contamination, it is also found to be compliant to regulations and cost saving. Different types of tank wall material have been taken into consideration to avoid corrosion issue, for example the high tensile fibre/polymeric composite [44]; nevertheless, this substance is not suitable to develop as a tank wall material alternative due to moisture absorption. An organic palm-made insulator has demonstrated improved thermal insulation efficiency for the critical components of water tanks [45]; it could function as a thermal stress reliever under climate change stimulation.

A multidimensional membrane sensor mechanism was established to monitor gas availability, soil temperature and building composition strain parameter [46]. To provide detailed CO, storage surveillance, the sensor measurement was validated through field application. By Coupled Euler-Lagrange exploiting 3-D simulation, material stress and liquid sloshing height was exhibited to be inversely proportional to liquid level and height-to-radius ratio [47]. In order to optimize water tank storage design, an extensive product life cycle assessment has been performed [48]. The major environmental factors were determined to be tank and containment material, specifically, tank positioning, geometry and volume setting. Utilizing the conductive nature of petrol contaminants, the Electrical Impedance Tomography (EIT) technique was used to project underground splitting area [49]. The responses from buried electrodes are visualized via acquisition of a local projective conductivity image method.

A mobilized robot with an attached olfaction device was simulated to perform various tasks within a toxic enclosure [50]. Modelling results show that the four-wheeled device was capable of collecting samples without any movement constraints; it is convenient to investigate any chemical reaction process between interior parts of UST and its content. Spatial temperature measurement of buried enclosures has been conducted using spiral shape ultrasonic guided waves (UGW) [51]. Compared to junction-based thermocouple, the piezo-electric crystal sensors are preferred in flammability warning because they are more effective, robust and less expensive.

# 2.2 Petrol and Hydrocarbons Detection Techniques

On the other hand, prioritized consideration has been given to petrol exposure resulting from operational processes due to concerns of populous petrol stations in urban areas. Analytical evaluation suggests that release of petrol fuel in liquid-gaseous form happens during storage and transportation, together with harmful anti-

knocking additives (benzene, lead, Methyl tertiary butyl ether (MTBE) and oxygenate) spreading into surrounding ground, water and open space. The open atmosphere measurement sampled at petrol stations indicates the existence of a high toxic mixture made up of benzene, formaldehyde, and hydrogen sulphide at a level higher than allowable limits [52]. Hence, the option of exploiting volatile hydrocarbon agent's fused passive vapour in UST defect monitoring was considered [53]. It is worth mentioning that leakage detection rate is dependent on vapour concentration in this case.

Further, the prospect of employing infused fuel oxygenate in groundwater motion tracing and gasoline contamination level was explored [54]. By referring to MTBE thermodynamic and dispersion data, the spill dissipation rate and biodeterioration of material was verified using 3-D inverse modelling. In other words, the effectiveness of remedial action on contamination was governed by the MTBE solubility rate in water source [55]. Additionally, the correlation between MTBE concentration, degradation in progress and loss of dilution charge over period was ascertained [56]. In Thailand, the volume of volatile fuel organic compounds (VFOC) at petrol station space areas were computed and visualized in an isoconcentration contour map to display the distribution of evaporated benzene and toluene [57]. As a result, a significant profile was observed at UST inlet points.

By recruiting sulphate as the electron acceptor in a groundwater treatment experiment, toluene demonstrated a maximum reduction in percentage, subsequently followed by benzene and MTBE [58]. However, the effectiveness of hydrocarbon bioremediation lessens as microbial levels become reduced over time. The soil and groundwater sample data around a petrol station was evaluated using hydrocarbon indices and principal component analysis (PCA) method to determine the effect of related operational activity on the intermidate environment [59]. Correspondingly, the pollution rate due to UST fuel leakage was correlated to VFOC and diesel range organics (DRO) readings. The prospect of utilizing a half-life dissipation model in estimating MTBE (which remains in aquifer over time) has been explored [60]. The predicted gasoline oxygenate concentration rate via first order kinetics equation matched real-time field measures; hence, it is applicable for public water supply damage severity mapping.

A novel carbon nanotube (CNT) sensor system was purposely designed with nanocomposite material to cater a violent underground surveillance [61]. The sensitivity of the aforementioned sensory mechanism is enhanced with the existence of time-varying parameters such as soil compost, humidity, pressure and temperature in output matrix. In order to deduce total release petrol hydrocarbons (TPHs) available in the vertical extent of soil, a 2-D grid view comprised of multiple plane was examined by polymerase chain reaction- denaturing gradient gel electrophoresis (PCR-DGGE) technique [62]. An analytical relationship between formations of microbial communities, leakage volume, texture and depth was defined based on field-test studies. An innovative in situ chemical oxidation (ISCO) method

was acquired to investigate the progress of aqueous treatment after UST gasoline leakage effects [63]. Potassium ferrate  $(K_2FeO_4)$  has been proven to be a more stable oxidizing agent in degrading active hydrocarbon migration elements (BTEX and MTBE) over diverse medium compositions (pH and concentration), as compared to permanganate and hydrogen peroxide.

A fuel leakage phase-change model was computed with respect to UST shape and surrounding area [64]. The contained liquid-gaseous proportion was projected into low explosion limit (LEL) indication to avoid fire accidents and eventually assist in efficient periodic corrective action selection. An electrical resistivity visualization technique was unveiled to target subsurface oil pollution spots around coastal cities in India [65]. This was realized by applying a set of multi-gas sensors to identify the hydrocarbon level in soil vapour sampling. Hydrocarbon spoil treatment outcomes has been compared extensively using land farming bioremediations in Nigeria [66]. Fertilizer was proven to be the most cost effective addition, over biochar, biosurfactant and other heterogeneous nutrient agents.

#### 2.3 Rule and Regulation Changes

As unpredictability in UST leakage increases, in terms of occurrence and damage severity, more stringent guiding principles in installation, operation, maintenance and safety have been proposed, amended and implemented by the authorities and professional organizations.

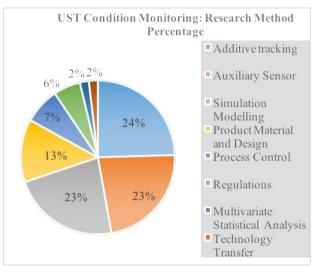
For example, The Environment Protection Agency (EPA) has updated a set of UST-related regulations which covers hardware reinforcement, increases the frequency of scheduled maintenance and requires the latest on-site certification for operators in charge [67]. In addition, the public has been motivated by the federal government of the United States to perform standardized monitoring practices revised by professional organizations. The imposed exemplar and guideline comprises the aspects of setting up, structural integrity assessment and health monitoring, operation and fulfilment activities, fault detection, corrosion protection methods and other general subjects.

Meanwhile, renowned industry manufacturer The Welding Institute (TWI) in the UK has implemented a wall thickness measurement criterion for pressure vessel product suggested by American Petroleum Institute (API) [68]: operating instructions for apparatuses in an ignitable environment [69]; and a reformed guideline for degrading steel products respective to the working environment [70]. Domestic standard regulations for USTs in Malaysia include: liquid storage steel tanks design specification [71]; an international guideline for welding procedures [72]; and an accredited welding technical qualification specifically for steel fusion [73].

Clearly, a series of proactive moves toward tightening up regulation lists serve as countermeasures in preventing and minimizing contamination problems, particularly against aging UST products. However, the UST-associated guidelines mentioned above cover a wide area and has been revised in a periodic manner to be flexible according to modern technology trends and multiple regions; thus, it is recommended to comply when applicable.

## 3 Challenges and Limitations

To summarize, it can be deduced that substantial research with the aim to upgrade the UST condition been conducted. monitoring model has specifically, the vast efforts incurred range from property extraction of tracking additives, auxiliary sensors, simulation modelling, product material research and design modification, process control, enforcement of a stricter standard compliance, multivariate statistical analyses, to matured technology transfer from proven case studies (Fig. 2). Evidently, the applications require a coherent collective field of knowledge with respect to the diverse physical form of contained material (Fig. 3), in order to overcome identified shortcomings in delivering sensitive inspection of USTs.



**Fig. 2.** UST Condition Monitoring Research Method Percentage

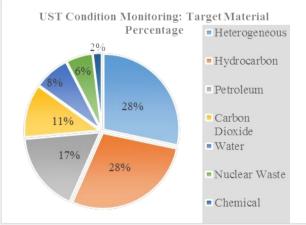
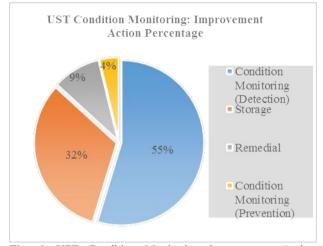


Fig. 3. UST Condition Monitoring Target Material Percentage

Nonetheless, obviously the present research direction has an emphasis on contaminant remedial action and leakage detection (Figure 4). While remedy effectiveness remains in question, fault detection capability means that the condition monitoring process is capped at lower levels one and two [74,75]. Without the ability to perform fault severity calibration and predict a product's lifespan, there remains insufficient information provided to understand the situation behind prior leakage, and it is too late if the damage is done. Furthermore, this statement is confirmed by the numerous health issues reported on petrol station assistants [57]; pollution prevention strategies opt for better cost-saving, energy conservation and health care measures [76] after a thorough hydrocarbon leakage evaluation.



**Fig. 4.** UST Condition Monitoring Improvement Action Percentage

Review on vibration structural health monitoring [77] encourages the exploration of signal response to utilize its fundamental statistical pattern recognition in developing advanced model- or non-model-based system identification. Analogous to vibration, a non-destructive evaluation (NDE) signal responds in an identical manner: the amplitude of waveform energy reflects the existence of abnormal events. Typically, statistical analysis is compatible with waveform interpretation due to its attribute's simplicity. However, it is observed that the trade-off relationship between the complexity of condition monitoring model and its accuracy are nontrivial. In general, simulation modelling supported by a combination of detailed theoretical background and mathematical settings will generate more precise performance, but it is computationally tedious. On the contrary, a plain, direct model could face a bottleneck when analysing complicated situation such as simultaneous monitoring and weighting of abundant signals. Comparatively, outlier detection can be achieved by extracting fundamental vibration features and applying it to techniques such as statistical process control (SPC) [78], adaptive template matching (ATM) [79], wavelet transform (WT) [80], or Fourier Transform [81], but the aforementioned methods are far away from mimicking reality and demand human supervision.

Based on the above reasoning, the following research concentrates on the necessity and fulfilment of machine learning algorithms by making use of NDE signalextracted features. By means of gaining sharp and retentive pattern-recognition memory, improvement is anticipated for the condition monitoring ability by developing a multi-fault classification model for USTs, labelling the severity scale and predicting the lifecycle of the product altogether.

#### 4 Recommendation

#### 4.1 Availability of NDE and its Advantages

As mentioned in the previous section, several NDE techniques have been inquired to address drawbacks introduced by the current trend. NDE is favourable since it possesses numerous advantages over conventional practice in identifying structural integrity over time. Similar to x-ray scanning in the medical sector, NDE signals are intended to detect an anomaly and pinpoint its position within the effective scanning area, with unlimited number of testing trials. Interpretation of encoded NDE signals is always paramount, though laborious. Hence, practising suitable NDE techniques for a unique case study is essential in pursuance of potential ability, and it can be reflected from multiple factors: parameter setting, sensitivity, adaptability, compatibility, and ease of implementation. Because of the considerable numbers in the NDE list, only choices that fits the required criteria on paper will be discussed, including ultrasonic guided wave (UGW) and acoustic emission

Ultrasonic guided wave technique is a branch of ultrasonic testing (UT) which release low frequency sound energy (50 kHz-200 kHz) mainly for cylindrical shape cross sectional and material characterization inspection purposes [82,83] and it has been extended to other complex shapes [84,85]. It is expert in long distance inspection owing to the capability of an induced stress wave to travel along the specimen's boundary. Since it is an active pulse/echo method, the pulse emitter and receiver of an UGW are typically attached to a material surface alongside each other; waveform signals created by a set of electronic pulse-driven transducers embeds into specimen and propagates in perpendicular directions.

When UGW eventually encounters discontinuity such as circumference variation, material properties and grains difference, propagating energy is reflected. The reflecting amplitude (A-scan) and shape (C-scan) express the extent of dissimilarities in size and orientation respectively; while the location of the reflector is measured from either frequency signal or time of flight (TOF). Nevertheless, the proficiency of UGW is slightly hindered by its own nature. Researchers has been aiming to overcome gaps concerning UGW's signal intensity, which diminishes after endured severe travel distance due to attenuation activities [86,87]; and its insensitivity to axial anomaly, which appears to be coincide with the travel direction of signal [88].

Contrary to any other common NDE techniques, acoustic emission is well-known as a passive approach since it anticipates signal waves produced by specimens

themselves, instead of putting effort into creating energy for feedback [89,90]. Fundamentally, under continuous, repetitive stress conditions (tensile, compressive, shear, bending and torsion), the mechanical properties of a specimen will experience alteration over time and breakdown when the force applied exceeds the sustainable limit. When failings such as deformation and fatigue arise, AE-encoding sensors concentrate on converting high-frequency acoustic stress waves (15 kHz-300 kHz) as a result of local loaded elastic kinetic energy discharge by discontinuities, into amplified electronic signals. The preliminary AE waveform proportionally describes the size and speed of defects; with the help from initiative data processing, it is suitable to monitor changes of a mechanical loaded structure, locate and identify incurred damages. Secondary forces such as friction, which interfere in the signal-to-noise (SNR) ratio remain a doubt in AE implementation [91].

It is of profound importance to recognize that UGW and AE holds different characteristics yet are superior in their own ways. It has been observed that UGW is indicated in elongated inspection areas, complex shapes and uncompromising environments [92-96], while AE is more suited to dynamic and mechanical applications [97-102]. That being said, practicing the above-mentioned NDE technique solely in UST monitoring is foreseen to be problematic due to individual distinctive features. For AE alone, inconsistency of mechanical stress applied on different UST body segments could lead to neglect of the upper segment, while UGW could overlook laminations and porosities, as well as uniform corrosion and erosion when considering negligible cross-sectional differences in range.

For better evaluation efficiency, the signal fusion approach has been offered in the interest of a diverse interpretation perspective [103,104]. For USTs in particular, the signal fusion concept suggests that both AE and UGW signals be emitted from adjacent directions, merging to forge a mesh-like screening field in favour of blind spot minimization. Besides, it is obvious that raw NDE signals require comprehensive numerical review with regards to identifying anomalies symptoms of anomalies and elimination of false alarms in automated mode [105].

#### 4.2 UST Condition Monitoring Model Package

The NDE signal plays a vital role as input signal in the UST model evaluation which could be separated into three main intermediates: material screening, signal processing and machine learning fault classification (Figure 5). With UST as the target, NDE signals react to stress-strain tabulation, cross sectional dissimilarity, liquid level contents and the amount of tank bottom settlement during material screening process without injuring the product structure.

The raw signals obtained from respective sensors mounted at appropriate locations carry little meaning without diagnosis from relevant signal processing algorithms. By applying noise reduction, feature

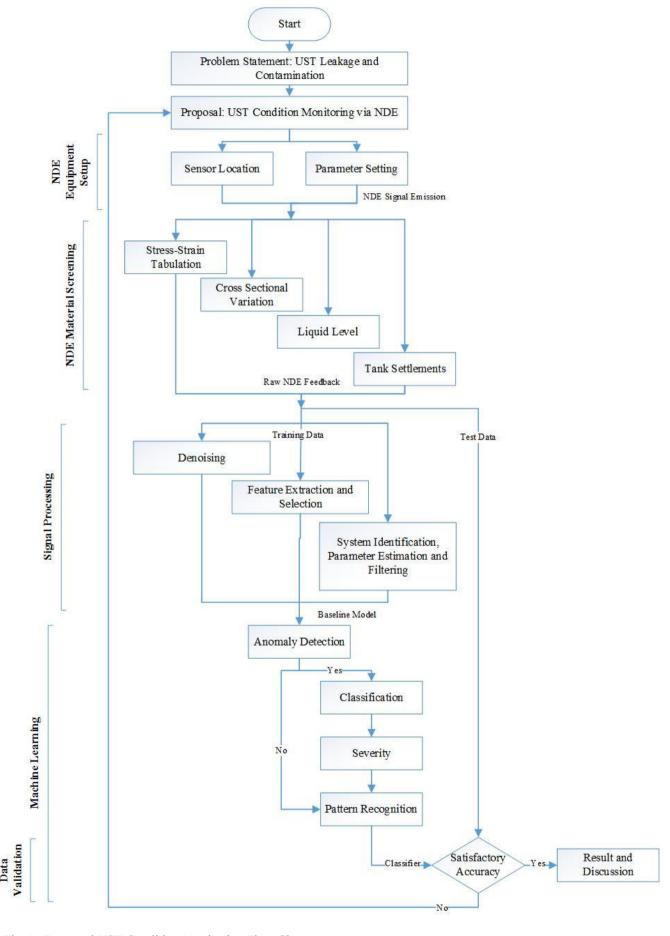


Fig. 5. Proposed UST Condition Monitoring Flow Chart

extraction, system identification, parameter estimation and filtering methods [106,107], the aim is to increase the SNR ratio and form a baseline mathematical equation to determine the relationship between signal response and product properties under various states. Other benefits consist of establishing strategic sensor placement to avoid bulky instruments and degraded performance caused by overfitting [108]; this reduces uncertainties, and provides an overview on both UST black box characteristics and cost optimization.

Next, machine learning algorithms will be responsible for analysing the processed signal distribution representing the linear characteristic of extracted features via the pattern recognition mechanism [109]. By means of analytical and numerical reasoning, a machine learning algorithm tends to detect and memorize deviations as anomalous, classify anomaly type according to outlier properties and determine the degree of severity of a given state of affairs through baseline model comparison. The fitness of the supervised classifier will be appraised by testing the dataset revealed after training stage, using multi-fold crossvalidation to avoid bias [110]. The best performer with least forecast error will be obtained as predictor in integrated condition monitoring model.

Practically, a predicting model functions under the influence of uncertainties appearing in the form of measurement noise, quality of extracted features and model design [111]. Future trends of machine learning lie in artificial intelligence (AI) agents cascaded with automated optimization or probabilistic functions. Numerous case study implies that AI's use has been rewarding in NDE signal classification and prediction in terms of accuracy, sensitivity and automated system, with recursive Artificial Neural Network (ANN) [112], wavelet based Support Vector Machine (SVM) [113], Euclidean-SVM [114], Bayesian Belief Network trained 'statistical-physical' and 'hypothesis-generating' model [115], wavelet decomposition- continuous hidden markov model (CHMM) integration [116] amongst modern proposed techniques. Though it already displays an outstanding yield, the AI classifier can still be improved by incorporating uncertain variables into

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deterministic model using stochastic estimation [117-119].

#### 5 Conclusion

With the motivation to reduce the occasions of distasteful containment leakage, pollution and corrective action, a significant amount of review has been discussed with the motivation to reform the UST condition monitoring model. In response to needs, the NDE technique is considered to be a competitive option amongst condition monitoring techniques in terms of sensitivity, cost-effectiveness and ease of installation. In addition, the hypothetically UGW-AE signal fusion seems to be more promising compared to a single signal emission in delivering spatial information of an UST as a whole, while coordinating with difficult operating surroundings and product shape complexity. Furthermore, signal processing and machine learning algorithms are integrated into the condition monitoring model as tools to interpret the retrieved NDE input signal, and perform automated pattern recognition fault classification if any outlier is located.

However, the study was conducted based on theory and experience from different applications, thus implementation on actual UST is foreseen to be effortful and challenging. This includes but is not limited to determining the location of sensors, establishing coherence between a pair of NDE signals and algorithm, SNR, signal feature extraction and selection, separation of genuine faults and false alarms, and classifier accuracy.

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